Definition 1. Let X be a system of sets. X is *closed under arbitrary unions* iff $\bigcup U \in X$ for every subclass U of X. Let X is *closed under unions* stand for X is closed under arbitrary unions.