Definition 1. Let X be a system of sets. X is *closed under countable unions* iff $\bigcup U \in X$ for every nonempty countable subclass U of X.