Definition 1. Let X be a system of sets. X is *closed under powersets* iff $\mathcal{P}(U) \in X$ for every $U \in X$.