Definition 1. A *system of countably infinite sets* is a system of sets X such that every element of X is countably infinite.

Definition 2. A *system of countable sets* is a system of sets X such that every element of X is countable.

Definition 3. A *system of uncountable sets* is a system of sets X such that every element of X is uncountable.